



MIDTERM EXAMINATION

MTH101- Calculus And Analytical Geometry

Question No: 1 (Marks: 1) - Please choose one

If f is a twice differentiable function at a stationary point x_0 and $f''(x_0) < 0$ then f has relative At x_0

- ▶ Minima
- ▶ **Maxima**
- ▶ None of these

Note:Maxima(If Maxima refers to local maximum)

Question No: 2 (Marks: 1) - Please choose one

A line $x = x_0$ is called ----- for the graph of a function f if $f(x) \rightarrow +\infty$ or $f(x) \rightarrow -\infty$ as x approaches x_0 from the right or from the left

- ▶ Horizontal asymptotes
- ▶ None of these
- ▶ **Vertical asymptotes**

Question No: 3 (Marks: 1) - Please choose one

A line $y = y_0$ is called a for the graph f if $\lim_{x \rightarrow +\infty} f(x) = y_0$ or $\lim_{x \rightarrow -\infty} f(x) = y_0$

- ▶ Vertical asymptotes
- ▶ Horizontal asymptotes
- ▶ **None of these**

Question No: 4 (Marks: 1) - Please choose one

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According to Power-Rule of differentiation, if $f(x) = x^n$ where n is a real number, then

$$\frac{d}{dx}[x^n] =$$

- ☐ x^{n-1}
- ☒ $n x^{n-1}$
- ☐ $n x^{n+1}$
- ☐ $(n-1)x^{n+1}$

Question No: 5 (Marks: 1) - Please choose one

$$y = \frac{1}{1-x} \quad \frac{dy}{dx} =$$

If _____ then

- ☐ 1
- ☒ -1
- ☐ $\frac{1}{(1-x)^2}$
- ☐ $\frac{-1}{(1-x)^2}$

Question No: 6 (Marks: 1) - Please choose one

$$\text{If } xy = 4 \text{ then } \frac{dy}{dx} =$$

- ☐ 0
- ☐ $\frac{-1}{x^2}$
- ☐ $\frac{4}{x^2}$
- ☒ $\frac{-4}{x^2}$

Question No: 7 (Marks: 1) - Please choose one

$$\text{If } 2x - y = -3 \text{ then } \frac{dy}{dx} =$$

- ☒ 2

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- ☒ -2
- ☐ 0
- ☐ -3

Question No: 8 (Marks: 1) - Please choose one

$$\frac{d}{dx}[\sec x] = \underline{\hspace{2cm}}$$

- ☐ $\frac{1}{1 + \sin^2 x}$
- ☐ $\frac{-\sin x}{1 + \sin^2 x}$
- ☐ $\frac{1}{1 - \sin^2 x}$
- ☒ $\frac{\sin x}{1 - \sin^2 x}$

Question No: 9 (Marks: 1) - Please choose one

$$30^\circ = \underline{\hspace{2cm}}$$

- ☐ $\frac{\pi}{3}$
- ☐ $\frac{\pi}{4}$
- ☒ $\frac{\pi}{6}$
- ☐ $\frac{\pi}{2}$

Question No: 10 (Marks: 1) - Please choose one

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Consider a function $h(x)$ and a constant c then

$$\frac{d}{dx}((c) \{h(x)\}) = \underline{\hspace{2cm}}$$

► 0

► $\frac{d}{dx}(h(x))$

► $\frac{d}{dx}(h(cx))$

► $c \frac{d}{dx}(h(x))$

Question No: 11 (Marks: 1) - Please choose one

$$\frac{d}{dx}[\operatorname{cosec} x] = \underline{\hspace{2cm}}$$

► $\frac{1}{1 + \cos^2 x}$

► $\frac{-\cos x}{1 - \cos^2 x}$

► $\frac{-\cos x}{1 - \cos^2 x}$

► $\frac{1}{1 - \cos^2 x}$

Question No: 12 (Marks: 1) - Please choose one

Chain rule is a rule for differentiating _____ of functions.

► **Product**

► Sum

► Difference

► Composition

Question No: 13 (Marks: 1) - Please choose one

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$$\frac{d}{dx}[x^n] = nx^{n-1}$$

The power rule, _____ holds if n is _____

- ▶ **An integer**
- ▶ A rational number
- ▶ An irrational number
- ▶ All of the above

Question No: 14 (Marks: 1) - Please choose one

Let a function f be defined on an interval, and let x_1 and x_2 denote points in that interval. If $f(x_1) < f(x_2)$ whenever $x_1 < x_2$ then which of the following statement is correct?

- ▶ **f is an increasing function.**
- ▶ f is a decreasing function.
- ▶ f is a constant function.

Question No: 15 (Marks: 1) - Please choose one

If $f''(x) > 0$ on an open interval (a,b), then which of the following statement is correct?

- ▶ **f is concave up on (a, b).**
- ▶ f is concave down on (a, b).
- ▶ f is linear on (a, b).

Question No: 16 (Marks: 1) - Please choose one

If $f''(x) < 0$ on an open interval (a,b) then which of the following statement is correct?

- ▶ f is concave up on (a, b).
- ▶ **f is concave down on (a, b)**
- ▶ f is linear on (a, b).

Question No: 17 (Marks: 1) - Please choose one

If $x > 0$ then $\frac{d}{dx}[\ln x] =$ _____

- ▶ 1
- ▶ x
- ▶ $\frac{1}{x}$
- ▶ $\ln \frac{1}{x}$

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Question No: 18 (Marks: 1) - Please choose one

If $b > 0$ then $\frac{d}{dx}[b^x] =$ _____

▶ 0

▶ xb^{x-1}

▶ $\ln b$

▶ $b^x \ln b$

Question No: 19 (Marks: 1) - Please choose one

Let $y = (x^3 + 2x)^{37}$. Which of the following is correct?

▶ $\frac{dy}{dx} = (37)(x^3 + 2x)^{36}$

▶

▶ $\frac{dy}{dx} = 111x^2(x^3 + 2x)^{36}$

▶

▶ $\frac{dy}{dx} = (111x^2 + 74)(x^3 + 2x)^{36}$

▶

▶ $\frac{dy}{dx} = (111x^2 + 74)(x^3 + 2x)^{38}$

▶

Question No: 20 (Marks: 1) - Please choose one

What is the base of natural logarithm?

▶ 2.71

▶ 10

▶ 5

▶ Any real number

Question No: 21 (Marks: 1) - Please choose one

Let x_0 be critical points of the function f . Those critical points for which $f'(x_0) = 0$ are called _____ of f

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- ▶ Local points
- ▶ End points
- ▶ **Stationary points**

Question No: 22 (Marks: 1) - Please choose one

$$\log_b a^r = \underline{\hspace{2cm}}$$

- ▶ $a \log_b r$
- ▶ $r \log_b a$
- ▶ $\frac{\log_b a}{\log_b r}$
- ▶ $\log_b a + \log_b r$

Question No: 23 (Marks: 1) - Please choose one

$$\log_b \frac{1}{c} = \underline{\hspace{2cm}}$$

- ▶ $\log_b c$
- ▶ $1 - \log_b c$
- ▶ $-\log_b c$
- ▶ $1 + \log_b c$

Question No: 24 (Marks: 1) - Please choose one

$$\log_b \frac{1}{t} = \underline{\hspace{2cm}}$$

- ▶ $\log_b t$

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- ▶ $1 - \log_b t$
- ▶ $1 + \log_b t$
- ▶ $-\log_b t$

Question No: 25 (Marks: 3)

If $f(x) = x^4 - 8x^2$, determine all relative extrema for the function. Using First Derivative Test.

Solution:

$$f = x^4 - 8x^2$$

$$f' = 4x^3 - 16x$$

$$f' = 0$$

$$4x^3 - 16x = 0$$

$$x(4x^2 - 16) = 0$$

$$x = 0$$

$$4x^2 - 16 = 0$$

$$x^2 = \frac{16}{4}$$

$$x^2 = 4$$

$$x = \pm 2$$

Relative extrema $(0, \pm 2)$Ans

Question No: 26 (Marks: 5)

Differentiate $y = x^{-2}(4 + 3x^{-3})$

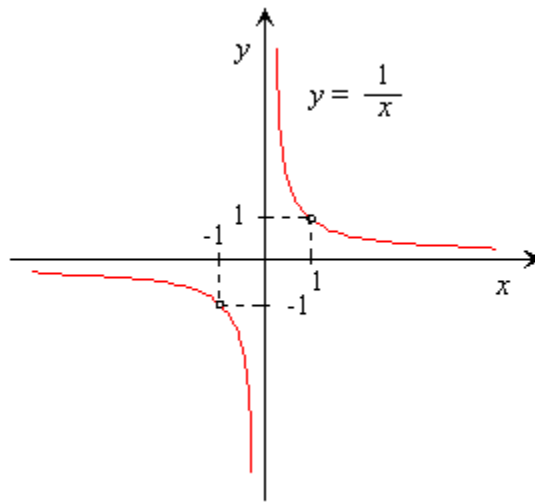
Solution:

$$\begin{aligned}y &= 4x^{-2} + 3x^{-3} \cdot x^{-2} \\&= 4x^{-2} + 3x^{-5} \\\frac{dy}{dx} &= 4 \frac{d}{dx}(x^{-2}) + 3 \frac{d}{dx}(x^{-5}) \\&= 4(-2)x^{-2-1} + 3 \frac{d}{dx} - 5x^{-5-1} \\&= -8x^{-3} + (-15x^{-6}) \\\frac{dy}{dx} &= -8x^{-3} - 15x^{-6} \dots \dots \text{Ans}\end{aligned}$$

Question No: 27 (Marks: 10)

$$f(x) = \frac{1}{x}$$

Determine the intervals in which the graph of the function is concave upward or downward.



Solution:

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$$f(x) = \frac{1}{x}$$

$$f'(x) = -\frac{1}{x^2}$$

X	1	2	3	4
F(x)	-1	-0.25	-0.11	-0.625

Conclusion:

$f'(x)$ is increasing when x is from $(0, \infty)$

so,

It is concave up.

$f'(x)$ is decreasing when x is from $(-\infty, 0)$

so,

It is concave down